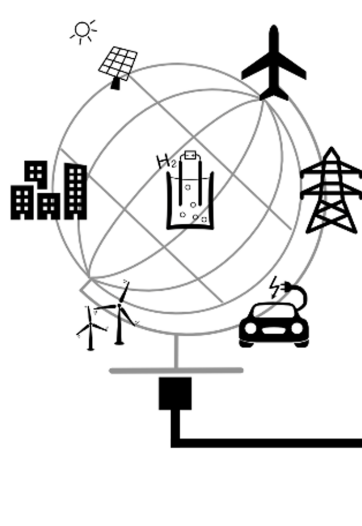
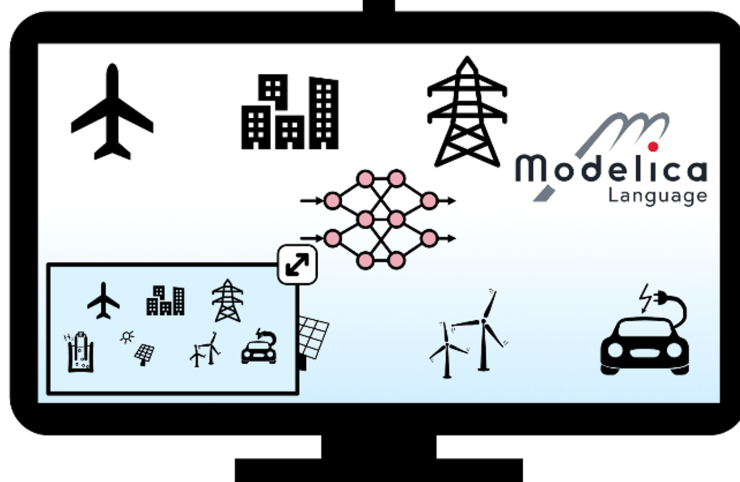




ITEA4 22013



Open standards for
Scalable Virtual Engineering
and Operation



Deliverable D6.3

State-of-the-Art Analysis

Lena Buffoni, Oliver Lenord, Lars Mikelsons, Martin Otter, Robert
Hällqvist

Version v3, July 1, 2026

Table of Contents

1. Modelling standards and software for digital twins.....	4
References.....	6
2. Multi Physics Simulation.....	6
3. Artificial intelligence for modelling and simulation.....	8
References.....	9
4. Credible digital twins.....	10
References.....	11
5. Uncertainty Quantification for Model Credibility.....	11
References.....	12

Project Acronyms

Acronym	Description
AI	Artificial Intelligence
COP	Coefficient of Performance
CPS	Cyber Physical System
CSP	Credible Simulation Process
DAE	Differential-algebraic equation
eFMI	Functional Mock-up Interface for embedded systems
FMI	Functional Mock-up Interface (standard for model exchange and co-simulation)
FMI component	A model in FMI format (= FMU)
FMU	Functional Mock-up Unit (= an FMI component)
HVAC	Heating, Ventilation and Air Conditioning
LOTAR	Long Term Archiving and Retrieval
LSS	Large-scale System
M&S	Modeling and Simulation
Modelica	Standard for modelling of cyber-physical systems
MosSEC	Modelling and simulation information in a collaborative system engineering context
MiL/SiL/HiL	Model/Software/Hardware in the Loop
NeuralODE	Ordinary Differential Equation, where a Neural Network (NN) defines its derivative function
NN	Neural Network
OD	Operational Domain
ODE	Ordinary Differential Equation
ONNX	Open Neural Network Exchange standard
PeN-ODE	Physics enhanced Neural ODE
PINN	Physics-informed Neural Network
SSP	System Structure and Parameterization (standard for connected FMUs)
UQ	Uncertainty Quantification

Acronym	Description
VV&UQ	Verification, Validation, and Uncertainty Quantification

From Full Project Proposal

ID	Type	Description	Due Month	Access
D6.3	Doc	Update of the ITEA "Living Innovation Roadmap" - will be iteratively delivered, e.g. with each PPR	recur.	Public

1. Modelling standards and software for digital twins

OpenSCALING will improve simulation-based processes rendering improved development of modelling and simulation applications such as scalable digital twins. One essential part are extensions of the following existing modelling standards that are in wide-spread use for the development of digital twins and are utilized to describe and to exchange dynamic multi-domain models, in particular from the mechanical, electrical, thermal, fluid, control, energy, building, automotive, aerospace domains. The underlying mathematical description are differential, algebraic and discrete equations:

- The [Modelica language](#) standard defines an open object-oriented language with 2-dim. object diagrams to model complex, dynamic systems on a high level. Modelica supports modelling with acausal connections of components defined by first principle equations. This standard has been developed since 1997, it is currently supported by [> 10 tools](#), and it is in widespread industrial use. Modelica tools support export of causal Modelica models as FMI compliant components known as Functional Mock-up Units (FMUs) (see next item). A large class of advanced Modelica libraries has been developed in the [ITEA EUROSYSLIB](#) project. Developments towards decarbonized energy systems for buildings, district energy systems and factories are often performed with the large, open source Modelica [Buildings library](#). Furthermore, the DLR developed Modelica library Thermo Fluid Stream (TFS) was made publically available in 2022 [<https://github.com/DLR-SR/ThermofluidStream/releases>] and it is emerging as particularly useful for modelling of thermo-fluid systems in, for example, the aerospace domain.
- [FMI \(Functional Mock-up Interface\)](#) is the leading, open standard to exchange dynamic models on a low level using a combination of (a) an XML-File to define the interface of a parameterized input/output block, (b) a dynamic link library to define the executable code that is accessed via a C-API, and (c) other resources all packed together in a zip-file. This standard was developed in the [ITEA MODELISAR](#) project and was afterwards further improved ([Blo2012], [Jun2021]). It is supported by [> 180 tools](#) and plays a key role in many industries for collaborative workflows and comprehensive cross-domain system level analysis, optimization and virtual tests. The FMI standard was recently extended to support the definition of layered standards, which allow to specify specific subsets of standards for domain or use-case specific applications ([Ber2023]).
- The [SSP \(System Structure & Parametrization\)](#) open standard is used to define complete systems consisting of one or more connected FMI (or Modelica) components including their parameterizations. It is supported by nearly [10 publically available tools](#). A major standard upgrade was achieved in 2025 with the release of SSP 2.0. This

version harmonizes Modelica with SSP supporting e.g., acausal components, supports the latest version of the FMI standard (3.0) and allows for incremental model development according to the needs of the OpenSCALING project.

Furthermore, developments performed in the [SetLevel](#) project extend SSP with quality assessment information to support a [Credible Simulation Process Framework](#)[\[Ah2022\]](#) [\[HMH2025\]](#). This work rendered a layered standard on top of FMI and SSP named [SSP LS-Traceability](#). SSP LS-Traceability allows models and simulators to be annotated with life-cycle information such that the portable containers evolve from being mere snapshots in time of an intended realization. The first tools with SSP LS-Traceability support are emerging and tool vendors such as Dassault Systemes with e.g., [Dymola](#) and eXXellent solutions with e.g., [easySSP](#) are offering incrementally expanded support.

- [eFMI \(Functional Mock-up Interface for embedded systems\)](#) is a recent open standard intended as exchange format for workflows and tool chains from physical models to embedded production code. An eFMI component is FMI compliant and can therefore be simulated by FMI tools to perform Software-in-the-Loop testing. Utilizing an eFMI component on an embedded device requires however dedicated tool support for eFMI. This standard was developed in the [ITEA EMPHYSIS](#) project ([\[Len2021\]](#)). The first tools with eFMI support are currently coming to the market.
- The [ISO 10303-243:2021 MoSSEC \(modelling and simulation information in a collaborative system engineering context\)](#) standard is an industrial effort to make progress in the representation of the elements “that together comprise a set of “results” for a study including the audit-trail of what is to be done, and what has been done, and evolution”, enabling “the representation of the definitions of models and key values that are part of the modelling” among others to allow the proper reuse of simulation models in a collaborative system engineering environment. Currently, some initial reference implementations can be found in the standard. [LOTAR \(Long Term Archiving and Retrieval\)](#) is an international consortium with the prime objective to create and deploy the EN/NAS 9300 series of standards for long-term archiving and retrieval of digital data in the aerospace domain. The LOTAR MBSE workgroup suggests the usage of Modelica, FMI and SSP as a basis ([\[Coi2021\]](#)).

Other important tools for simulation-based processes and digital twins:

- [MATLAB](#) and [Simulink](#) to design, simulate and deploy input/output blocks and especially controllers.
- [Simscape](#) to model and simulate multi-domain physical systems.
- [JuliaSim \(rebranded as Dyad\)](#) to model and simulate multi-domain physical systems within the Julia ecosystem. The available model libraries are currently very limited when compared with Modelica or Simulink/Simscape. Advantage is the easy

combination with many open-source Julia packages, e.g., for error propagation or machine learning.

- Open source packages from the [Julia ecosystem](#) such as [ModelingToolkit.jl](#) or [Modia.jl](#) provide high-level descriptions of multi-domain models, however lack a graphical user interface. The available model libraries are currently very limited when compared with Modelica or Simulink/Simscape. Advantage is the easy combination with many open-source Julia packages, e.g., for error propagation or machine learning.

References

- [\[Blo2012\]](#): Blochwitz, Otter, Akesson, Arnold, Clauß, Elmqvist, Friedrich, Junghanns, Mauss, Neumerkel, Olsson, Viel (2012): Functional Mock-up Interface 2.0: The Standard for Tool independent Exchange of Simulation Models. [DOI 10.3384/ecp12076173](#).
- [\[Jun2021\]](#): Junghanns, Blochwitz, Bertsch, Sommer, Wernersson, Pillekeit, Zacharias, Blesken, Mai, Schuch, Schulze, Gomes, Najahfi (2021): The Functional Mock-up Interface 3.0 - New Features Enabling New Applications. [DOI 10.3384/ecp2118117](#).
- [\[Ber2023\]](#): Bertsch, Süvern, Sommer, Schuch, Reim, R., Menne, Junghanns, Blochwitz, Blesken, Täuber (2023): Beyond FMI - Towards New Applications with Layered Standards. Proceedings of the 15th International Modelica Conference 2023, Aachen, October 9-11. [DOI 10.3384/ecp204381](#).
- [\[Len2021\]](#): Lenord, Otter, Bürger, Hussmann, Le Bihan, Niere, Pfeiffer, Reicherdt, Werther (2021): eFMI: An open standard for physical models in embedded software. [DOI 10.3384/ecp2118157](#)
- [\[Coi2021\]](#): Coïc, Murton, Mendo, Williams, Tummescheit, Woodham (2021): Modelica, FMI and SSP for LOTAR of Analytical mBSE models: First Implementation and Feedback. [DOI 10.3384/ecp2118149](#).
- [\[Ah2022\]](#): Ahman, Le, Eichenseer, Steinmann, Benedikt, (2022): Towards Continuous Simulation Credibility Assessment. <https://doi.org/10.3384/ecp193171>].
- [\[HMH2025\]](#): Hans-Martin Heinkel and Martin Geissen, (2025): Simulation Credibility Assessment. https://www.prostep.org/fileadmin/prod-pay-download-8c1d/WhitePaper_SmartSE_Simulation-Credibility-Assessment_2025_V7.0_FINAL_Titel.pdf

2. Multi Physics Simulation

OpenSCALING addresses the field of system simulation which is characterized by the interaction of sub-models from different physical domains. Current industrial trends result in new challenges for multi-physics simulations:

- Automotive: HVAC-systems of electric vehicles do not provide a comfort function for the passengers only. Keeping the battery system at the right temperature level is essential for a correct function and a long battery lifetime. In contrast to combustion engines which produce enough waste heat, electrical vehicles must generate extra heat which directly reduces the range. Heat pumps and very efficient HVAC-systems are countermeasures. This leads to more complex and larger multi-physics system models, which are challenges for simulation tools, and to higher requirements to the accuracy of models, which increases the modelling effort and requires expert knowledge.
- Buildings and Energy: Also, in these fields a trend to larger simulation models with more subsystems coming from different physical domains can be observed. The energy field has to consider the interactions between different kinds of energy production like fossil, wind and solar energy. State of the art buildings have multivalent sources for electrical energy, heating, and cooling which are coordinated by energy management systems. To assess the efficiency of such systems, simulations over the whole year are necessary to consider the seasonal weather effects. Simulation tools are confronted with large-scale models which have to be computed extremely fast.
- Aerospace: Modelling and simulation is, and has been, particularly relevant for design and development of aircraft and aircraft sub-systems. Modern aircraft are characterized by having tightly integrated and highly interconnected sub-systems. Modelling and simulation are, as a consequence, essential to capture and exploit emergent behaviour. Improved modelling and simulation capabilities, in terms of increased model predictive capability with a lower or reduced computational cost, will enable the development of more effective thermal management strategies and associated software. Such improvements will, in the end, result in the development of future aircraft that meet increasingly demanding performance requirements with a reduced environmental impact.
- All industries: The necessity to include sub-models from different domains leads to an increased exchange of simulation models via FMI. The concept of Terminals, introduced with FMI 3.0 in 2022, simplifies the error-proof interconnection of FMUs due to bus and physical connectors for the modeller. But the FMI 3.0 Terminals concept is based on causal connectors. The selection, which signal becomes an input or an output still needs to be negotiated between the involved parties. Inappropriate constellations lead to algebraic loops over large parts of the combined models which often leads to numerical problems and/or a reduction of the computational performance. The OpenSCALING innovation regarding acausal FMU-interconnections will significantly improve this situation.

3. Artificial intelligence for modelling and simulation

Following the rapid progress in the field of machine learning in computer vision, classification and further in the last decade, industrialization of these approaches and methodologies already happened or is ongoing. The topic of hybrid modelling, the use of machine learning as part of common simulation models, was initially raised in the 90s ([Psi1992], [Hon1992], [Joh1992]), however, has not been able to gain industrial relevance over the last decades. Progress in the field of AI hardware, as well as the further development and adaptation of algorithms for sensitivity analysis, have allowed this field of research to flourish once again today. Important contemporary works in this field where Neural ODEs in 2018 ([Che2018]) and physics-informed neural networks (PINNs) in 2019 ([Rai2018]).

In classical (engineering) modelling, the right-hand side of an ordinary differential equation (ODE) is generally represented as a symbolic expression derived from physical equations or mechanistic relationships. A Neural ODE is an ordinary differential equation, where a neural network defines the right-hand-side. If the right-hand-side is a combination of neural networks and physical equations no term has become established yet. Within OpenSCALING the term PeN-ODEs (Physics enhanced Neural ODEs) is used since these models can be trained with the same methods as Neural ODEs, however contain explicit physical formulations. In this way, for example, previously constant parameters can be replaced by NNs that can in principle depend on arbitrary other quantities. Another way to utilize NNs is to improve the state derivatives computed using physical equations to match measurement data before passing them to the ODE solver. The gradients with respect to the NN parameters, required for training, can either be computed using AD (Automatic Differentiation) through the solver or other sensitivity analysis methods for ODEs. In contrary, for PINNs the physical equations are used as a regularization term in the loss and the model itself is a NN without any physical equations. This difference can be in turn used to classify different approaches to integrate physical knowledge into hybrid models. Typically, using physical equations inside the model leads to a better extrapolation capability, especially in presence of (time-dependent) inputs. However, if low computational effort is favored often models without physical equations are employed. In recent years many approaches for generating such **surrogates** have been developed. However, method development, testing and validation is in most of the cases done using academic examples. Within project PHyMoS selected approaches, e.g., Proper Orthogonal Decomposition and MeshGraphNets, are investigated in industrial use cases. While great potential has been proven, upscaling to LSS results in unacceptable training times if no application specific measures are taken. After showing the potential of hybrid modelling in academia in recent years, this approach was evaluated in first use

cases among different domains from climate modelling, simulation of the human cardiovascular system ([Thu2021]) and modelling of fluid flows to driving simulation. Within the ITEA project UPSIM accuracy boosts up to 40% on validation data were shown for the hybrid modelling of a brake system as PeN-ODEs in form of a Neural FMU and comparable results for PeN-ODEs of a vehicle's vertical dynamics ([Thu2022]). The application of open standards like [ONNX \(Open Neural Network Exchange\)](#) starts to gain a larger community in Modelica, for example by the [SMArtInt Modelica library](#), developed by XRG-Simulation, and supported by Dymola and OpenModelica. These allow to integrate trained Neural Networks into Modelica models. A further step forward toward industrial-scale usage of PeN-ODEs is the publication of the layered standard for sensitivity analysis (LS-SA, ([Thu2025])), that provides an interface for gradient computation of FMUs, which is required to efficiently train new hybrid models. This serves as a foundation for training FMUs together with Neural Networks, e.g. as a NeuralFMU. This standard is currently being implemented by tool vendors, such as in Dymola by Dassault.

Moreover, recently, the question of uncertainty quantification (UQ) was also raised for hybrid modelling ([Psa2022]), however, an according methodology or toolset available for industry is missing.

Additionally, the usage of AI-Agents for supported modelling and simulation has been implemented in Modelica tools, e.g. in Dymola and Modelon Impact. OpenModelica currently develops an MCP-Server (model context protocol) to allow safe interaction with AI-Agents. Within the Julia language, the model editor [Dyad](#) for ModelingToolkit.jl also features an AI-Agent.

To conclude, it is shown that using AI in modelling has the potential to become the standard approach for complex systems. Since the start of the research project, there has been progress for quicker and wider adoption of hybrid modelling, i.e. by the development of the layered standard for sensitivity analysis (LS-SA), the SMArtInt library and the implementation of AI-Agents in Modelica tools. Adoption of UQ methods for according models respectively training methods that can handle large-scale systems are required to apply the available technology for credible models of complex systems.

References

- [\[Psi1992\]](#): Psychogios, Dimitris C. and Ungar, Lyle H. (1992): "A hybrid neural network-first principles approach to process modeling." *AIChE Journal*. DOI [10.1002/aic.690381003](#).
- [\[Hon1992\]](#): Hong-Te Su and N. Bhat and P.A. Minderman and T.J. McAvoy. (1992): "Integrating Neural Networks with First Principles Models for Dynamic Modeling." *IFAC Proceedings Volumes 25*. DOI [10.1016/S1474-6670\(17\)51013-7](#).

- [\[Joh1992\]](#): Johansen, Tor A. and Foss, Bjarne A. (1992): "Representing and Learning Unmodeled Dynamics with Neural Network Memories." 1992 American Control Conference. DOI [10.23919/ACC.1992.4792705](#).
- [\[Che2018\]](#): Chen, Ricky TQ, et al. (2018): "Neural ordinary differential equations." Advances in neural information processing systems. DOI [10.48550/arXiv.1806.07366](#)
- [\[Rai2018\]](#): Raissi, Maziar, Paris Perdikaris, and George E. Karniadakis. "Physics-informed neural networks: A deep learning framework for solving forward and inverse problems involving nonlinear partial differential equations". DOI [10.1016/j.jcp.2018.10.045](#).
- [\[Thu2021\]](#): Thummerer, Tobias and Tintenherr, Johannes and Mikelsons, Lars. (2021) "Hybrid modeling of the human cardiovascular system using NeuralFMUs". Journal of Physics: Conference Series. DOI [10.1088/1742-6596/2090/1/012155](#).
- [\[Thu2022\]](#): Thummerer, Tobias and Tintenherr, Johannes and Mikelsons, Lars. (2022) "NeuralFMU: Presenting a Workflow for Integrating Hybrid NeuralODEs into Real-World Applications". Electronics. DOI [10.3390/electronics11193202](#).
- [\[Thu2025\]](#): Thummerer, Olsson, Song, Gundermann, Blochwitz, Mikelsons (2025): LS-SA: Developing an FMI layered standard for holistic & efficient sensitivity analysis of FMUs. Proceedings of the 16th International Modelica & FMI Conference, September 8–10, 2025, Lucerne. DOI [10.3384/ecp218681](#).

4. Credible digital twins

In the [ITEA UPSIM](#) project several elements for credible digital twins are developed, such as the Credibility Development Kit. In the [SmartSE Recommendation](#) documentation, it is recommended to assess the credibility of a generic model resp. of a simulation with respect to Verification, Validation and UQ aspects using a dedicated Credibility Wheel. Such a credibility wheel is accessible e.g., from [easySSP](#). Partially, the [Credible Simulation Process Framework](#) from the [SetLevel](#) project is utilized that integrates simulation with SSP models into the development and quality assessment of automated driving functions. In both projects emphasis is on the management process to develop credible digital twins. There is a huge literature on other aspects of credible models, such as calibration, verification, validation, uncertainty analysis, sensitivity analysis, Monte Carlo Simulation, Design of Experiments etc... ([\[Law2019\]](#), [\[NAS2019\]](#), [\[Rie2021\]](#)). All these methods are typically not integrated in a modelling software. For example, the uncertainty information is usually defined in the tools that perform uncertainty analysis, and not in the models where the information naturally belongs to.

References

- [\[Psa2022\]](#): Psaros, Apostolos F., et al. "Uncertainty quantification in scientific machine learning: Methods, metrics, and comparisons." arXiv preprint arXiv:2201.07766 (2022). DOI [10.48550/arXiv.2201.07766](#)
- [\[Law2019\]](#): Law (2019): How to build valid and credible simulation models. DOI: [WSC40007.2019.9004789](#).
- [\[NAS2019\]](#): NASA 2019: NASA Handbook for Models and Simulations.
- [\[Rie2021\]](#): Riedmaier, Danquah, Schick, Diermeyer (2021): Unified Framework and Survey for Model Verification, Validation and Uncertainty Quantification. DOI [10.1007/s11831-020-09473-7](#).

5. Uncertainty Quantification for Model Credibility

The modern view of model credibility builds on the Verification, Validation, and Uncertainty Quantification (VV&UQ) framework: models must be verified for numerical correctness, validated against data, and presented with quantified uncertainty to support trustworthy decisions ([\[Roy2011\]](#)).

A recent survey across multiple industries makes the case for a unified VV&UQ view that covers different application areas, from finite-element models to cyber-physical systems, while keeping credibility evidence portable. Riedmaier et al. propose a modular framework that explicitly links VV&UQ activities to decision-making, highlighting the need for traceable artifacts and reusable evidence throughout a model's lifecycle ([\[Riedmaier2021\]](#)).

Two key developments now define state-of-the-art implementations:

- **Machine-interoperable traceability & process frameworks:** Extension mechanisms, such as layered approaches in FMI and the SSP Traceability standard, allow credibility information to be packaged with models in a consistent way. In addition, continuous credibility processes introduce checkpoints such as traceability, quality assurance, and review points, so that evidence of credibility can be built up and reviewed over time ([\[Ahmann2022\]](#), [\[Heinkel2021\]](#)). OD-aware traceability of model verification and intended use further supports automated relevance checks and scalable reuse in large simulation environments ([\[Rosenlund2025\]](#)).
- **Credibility-aware modelling and data stewardship.** On the modelling side, Otter et al. demonstrate how Modelica models can be extended with traceability, parameter

uncertainty, and calibration metadata using the open Credibility library, bringing credibility information closer to the model itself ([Otter2022]). On the data side, the FAIR principles (Findable, Accessible, Interoperable, Reusable) have become a central reference for managing simulation inputs, datasets, and results, with an emphasis on machine-actionable metadata that supports reuse and automation ([Wilkinson2016]).

One of the important focus areas is predictive capability: measuring whether a model can be trusted across its operational domain (OD), not only at validated points. Two main groups of metrics are used. Coverage-based metrics (for example, a modified nearest-neighbor metric) assess how well validation experiments cover the OD, discouraging results outside the tested range and helping to plan effective experiments ([Atamturktur2015]). Information-theoretic metrics, based on Shannon entropy and Kullback–Leibler divergence, compare distributions from simulations and experiments ([Shannon1949], [Kullback1951]). Recent aerospace studies combine both approaches to deliver OD-aware assessments of predictive capability based directly on validation experiments ([Hallqvist2023]).

In summary, the state of the art is converging on: (i) standards-centric packaging of UQ and credibility data (via layered standard extensions) to enable cross-tool reuse; (ii) process frameworks that integrate credibility into day-to-day simulation workflows; (iii) objective predictive-capability metrics that explicitly consider coverage and information content across the OD; and (iv) FAIR data stewardship and model-embedded credibility metadata to make the entire workflow reproducible and machine-actionable ([Roy2011], [Riedmaier2021], [Otter2022], [Wilkinson2016]).

References

- [Roy2011]: Roy, Christopher J., and William L. Oberkampf (2011): “A comprehensive framework for verification, validation, and uncertainty quantification in scientific computing.” **Computer Methods in Applied Mechanics and Engineering**, 200, 2131–2144. DOI 10.1016/j.cma.2011.03.016.
- [Riedmaier2021]: Riedmaier, Stefan, Benedikt Danquah, Bernhard Schick, and Frank Diermeyer (2021): “Unified Framework and Survey for Model Verification, Validation and Uncertainty Quantification.” **Archives of Computational Methods in Engineering**, 28(4), 2655–2688. DOI 10.1007/s11831-020-09473-7.
- [Ahmann2022]: Ahmann, Maurizio, Van-Thanh Le, Frank Eichenseer, et al. (2022): “Towards Continuous Simulation Credibility Assessment.” **Proceedings of the Asian Modelica Conference 2022**, 171–182. DOI 10.3384/ecp193171.
- [Heinkel2021]: Heinkel, H. M., and K. Steinkirchner (2021): **Credible Simulation Process – Simulation-based Engineering and Testing of Automated Driving**. [Link](#).

- [\[Rosenlund2025\]](#): Rosenlund, Erik, Robert Hällqvist, Robert Braun, and Petter Krus (2025): “Objectively Defined Intended Uses, a Prerequisite to Efficient MBSE.” **Proceedings of the American Modelica Conference 2024**, 29–42. DOI [10.3384/ecp20729](#).
- [\[Otter2022\]](#): Otter, Martin, Matthias Reiner, Jakub Tobolář, Leo Gall, and Matthias Schäfer (2022): “Towards Modelica Models with Credibility Information.” **Electronics**, 11(17):2728. DOI [10.3390/electronics11172728](#).
- [\[Wilkinson2016\]](#): Wilkinson, Mark D., Michel Dumontier, IJsbrand Jan Aalbersberg, et al. (2016): “The FAIR Guiding Principles for scientific data management and stewardship.” **Scientific Data**, 3:160018. DOI [10.1038/sdata.2016.18](#).
- [\[Atamturktur2015\]](#): Atamturktur, Sez, Matthew C. Egeberg, François M. Hemez, and Garrison N. Stevens (2015): “Defining coverage of an operational domain using a modified nearest-neighbor metric.” **Mechanical Systems and Signal Processing**, 50–51, 349–361. DOI [10.1016/j.ymssp.2014.05.040](#).
- [\[Shannon1949\]](#): Shannon, C. E. (1949): “A Mathematical Theory of Communications.” **The Bell System Technical Journal**, 27(3), 379–423.
- [\[Kullback1951\]](#): Kullback, S., and R. A. Leibler (1951): “On Information and Sufficiency.” **Annals of Mathematical Statistics**, 22(1), 79–86. DOI [10.1214/aoms/1177729694](#).
- [\[Hallqvist2023\]](#): Hällqvist, Robert, Magnus Eek, Robert Braun, and Petter Krus (2023): “Toward Objective Assessment of Simulation Predictive Capability.” **Journal of Aerospace Information Systems**, 20(3), 152–167. DOI [10.2514/1.I011153](#).